



# Properties of Special Quadrilaterals

## Student Activity

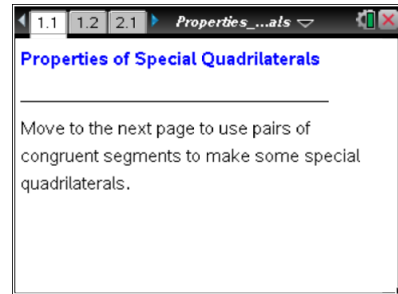
Name \_\_\_\_\_

Class \_\_\_\_\_

Open the TI-Nspire document

*Properties\_of\_Special\_Quadrilaterals.tns.*

In this activity, you will explore properties of some special quadrilaterals. In one part, you will use segments to build a quadrilateral. In another part, you will explore angle relationships. You will use your experiences to help make observations about the sides and angles in these special quadrilaterals.



Move to page 1.2.

Press **ctrl** **▶** and **ctrl** **◀** to navigate through the lesson.

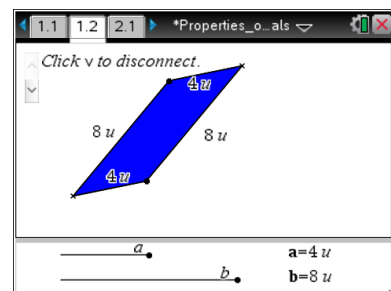
Press **ctrl** **tab** to move the cursor to the bottom portion of the screen.

1. Drag point  $a$  in the bottom portion of the screen to change the value of  $a$ , and describe what happens in the top portion of the screen.
2. Drag point  $b$  in the bottom portion of the screen to change the value of  $b$ , and describe what happens in the top portion of the screen.

Press **ctrl** **tab** to move the cursor to the top portion of the screen.

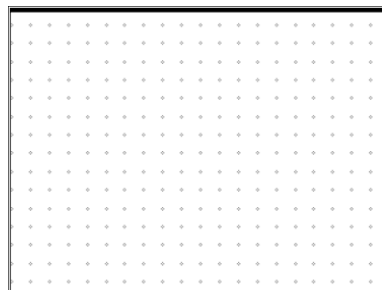
3. a. Move the segments to form a quadrilateral by following the steps:

- Pairs of segments can be moved by dragging the  $x$  found at their point of intersection (common endpoint).
- The angle between the connecting segments can be changed by dragging an endpoint that looks like this: ●.
- Final placement of segments can only be end-to-end.
- Move the segments and change the angle to get as close as you can to form a quadrilateral. Then press  $\wedge$  to connect.
- The goal is to have all four segments connected to one another to form a closed figure.

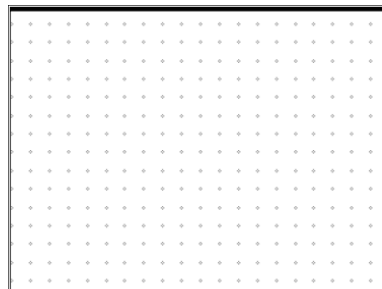




b. Sketch your results on the screen at the right.



4. a. Use the point of intersection  $x$  to drag and change the quadrilateral. Sketch your new quadrilateral.



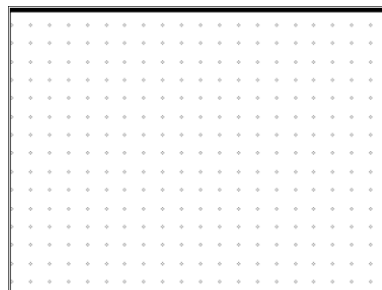
b. Compare and contrast your quadrilaterals in questions 3 and 4.

| Similarities | Differences |
|--------------|-------------|
|              |             |

5. In questions 1–4, you determined the lengths of the pairs of segments and then made a quadrilateral. Press **ctrl** **tab** to move to the bottom portion of the screen. Change the values of **a** and **b**, and observe the changes in the quadrilateral. Describe what happens to the quadrilateral as the values of **a** and **b** are changed.

**Move to page 2.1.**

6. Change the lengths in the bottom portion of the screen so that **a = b**. Press **ctrl** **tab** to move to the top of the screen and move the segments to form a quadrilateral. Sketch your results. What types of quadrilaterals can be made when all four segments are equal?





Move to page 3.1.

7. A special quadrilateral has been constructed that includes angle measurements.
- a. Drag a vertex other than  $S$  and record angle measurements in the chart at the right. Make a conjecture about the relationship of consecutive angles  $\angle P$  and  $\angle Q$ .

| $\angle P$ | $\angle Q$ |
|------------|------------|
|            |            |
|            |            |
|            |            |
|            |            |

- b. To display the measurements of the other two angles, press  $\wedge$  on the screen. Then drag a vertex. Make a conjecture about the measures of opposite angles  $\angle P$  and  $\angle R$ .

Move to page 4.1.

8. Find a quadrilateral that has been constructed using the intersection points of two pairs of parallel lines. Drag vertex  $A$ ,  $B$ , or  $C$ . Observe the lengths of the sides.
- a. What seems to be true about opposite sides of quadrilateral  $ABCD$ ? To display the measurements of the other two sides, press  $\wedge$  on the screen. Make a conjecture about opposite sides.
- b. Press  $\wedge$  on the screen to display angle measurements. Explain why consecutive angles  $\angle BAD$  and  $\angle ADC$  are supplementary.
- c. Explain why opposite angles  $\angle BAD$  and  $\angle DCB$  are congruent.
9. The quadrilaterals you have been exploring on all the pages of this activity are parallelograms.
- a. Why do you think they are called parallelograms?
- b. Renata says that in a parallelogram, the opposite sides are always parallel and congruent. Jerome says that in a parallelogram, each pair of consecutive angles is supplementary and opposite angles are congruent. Who is correct? Renata? Jerome? Both? Neither? Explain your reasoning.