



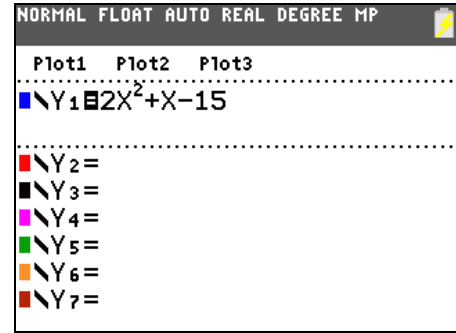
Using Symmetry to Find the Vertex of a Parabola

Student Activity

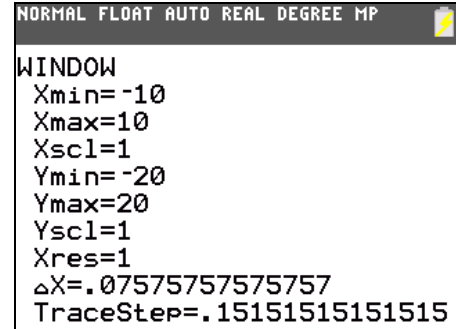
Name _____

Class _____

Consider the equation $y = x^2 + x - 15$. Press $\boxed{Y=}$ and enter the equation as shown.

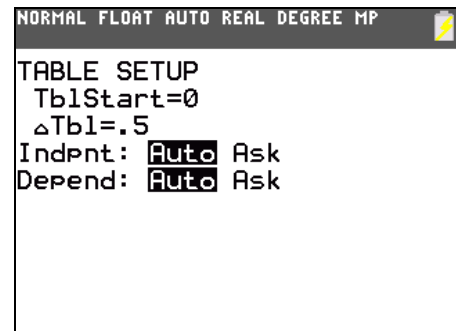


Press $\boxed{\text{GRAPH}}$. Take a moment to examine the graph. It would be helpful to be able to see the vertex. Press $\boxed{\text{WINDOW}}$ and adjust the window to show more space below the x-axis. Press $\boxed{\text{GRAPH}}$.



- Approximately where is the vertex of the parabola?
- What do you notice about the shape of the parabola?

The symmetry of a parabola should mean that for every value of y that the parabola takes on, there are two values of x that are paired with it. Press $\boxed{2\text{nd}} \boxed{\text{TABLE}}$. Examine the table and notice that there are no repeated values of y . Try adjusting the table set up to view more values of x . Press $\boxed{2\text{nd}} \boxed{\text{TBLSET}}$ and set the “change in table” to 0.5 as shown here.



Press $\boxed{2\text{nd}} \boxed{\text{TABLE}}$. Now, as expected, each y value is associated with two x values. Choose a pair of x -values that have the same y -value.

| X | Y1 | | | | |
|-----|-----|--|--|--|--|
| -5 | -15 | | | | |
| 0 | -15 | | | | |
| .5 | -14 | | | | |
| 1 | -12 | | | | |
| 1.5 | -9 | | | | |
| 2 | -5 | | | | |
| 2.5 | 0 | | | | |
| 3 | 6 | | | | |
| 3.5 | 13 | | | | |
| 4 | 21 | | | | |
| 4.5 | 30 | | | | |

X = -.5

Press $\boxed{2\text{nd}} \boxed{\text{QUIT}}$ to go to the Home screen. Average the two x -values by adding them together and then dividing the sum by 2.



Return to the table. Choose another pair of x -values that have the same y -value.

Press $\boxed{2\text{nd}} \boxed{[\text{QUIT}]}$ to go to the Home screen. Average the two x -values.

- What do you notice about the two averages so far?
- What significance might this number have?
- Using either factoring or the quadratic formula you should (or will) be able to find two x -values that have the y -value of zero for many parabolas.

Choose the two x -values that represent the zeros of this parabola using the table or another method.

| X | Y ₁ | | | | |
|-----|----------------|--|--|--|--|
| .5 | -14 | | | | |
| 1 | -12 | | | | |
| 1.5 | -9 | | | | |
| 2 | -5 | | | | |
| 2.5 | 0 | | | | |
| 3 | 6 | | | | |
| 3.5 | 13 | | | | |
| 4 | 21 | | | | |
| 4.5 | 30 | | | | |
| 5 | 40 | | | | |
| 5.5 | 51 | | | | |

X=2.5

Return to the home screen. Average the two x -values.

- What do you notice about these three averages? What significance might this number have?

Think about what it means to average two numbers on a number line. The average is the point **halfway** in between the numbers.

- If you fold the parabola and match up the symmetrical parts, what would be the point on the fold, or halfway in between?

To see what the significance of the value $x = -0.25$, examine the graph. Press $\boxed{\text{GRAPH}}$. Press $\boxed{\text{TRACE}}$. In "trace" mode, type $\boxed{(-)} \boxed{.}$ $\boxed{2} \boxed{5}$. Press $\boxed{\text{ENTER}}$.

- What point on the parabola have you found?

